

# **General Certificate of Secondary Education January 2013**

**Mathematics (Linear)** 

4365

Paper 1 Foundation Tier 43651F

# **FINAL**

Mark Scheme

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# **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

- **M** Method marks are awarded for a correct method which could lead to a correct answer.
- A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
- **B** Marks awarded independent of method.
- **Q** Marks awarded for quality of written communication. (QWC)
- **M Dep** A method mark dependent on a previous method mark being awarded.
- **B Dep** A mark that can only be awarded if a previous independent mark has been awarded.
- ft Follow through marks. Marks awarded following a mistake in an earlier step.
- SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
- oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as  $\frac{1}{2}$

# **Paper 1 Foundation Tier**

| Q    | Answer                 | Mark | Comments                            |
|------|------------------------|------|-------------------------------------|
|      |                        |      |                                     |
| 1(a) | (0)305, 1505, 5 past 3 | B1   | oe Ignore any reference to am or pm |

# Additional guidance

Accept colon, no gap shown, decimal point, comma in time notation

| 1(b) | Acute | B1 |   |
|------|-------|----|---|
| 1(c) |       |    | B2 Answer of 1125 or 1240<br>or (0)910 + 3 × 60 + 15 oe   |
|      | 12 25 | В3 | B1 1010 or 1110 or 1210 seen<br>or (0)925 or 1025 seen<br>or 3 × 60 + 15 oe<br>All times are oe |

#### Additional guidance

It is valid to add the time intervals in any order because they are asked for the final time and not the intermediate times so, for example, allow 1125 to come from adding 60 then 15 then 60

1125 and 1240 score B2 because they are commonly seen and both only have one error:

1125 is missing 60 mins and 1240 has two breaks

The equivalents for  $3 \times 60 + 15$  may be in hours or minutes (condone 3.15 (hours))

Condone any notation (words/ colons/ commas/ gaps etc) for time and ignore any reference to am or pm If the intermediate times are incorrect, then you need to see the addition of 60 (min) or 1 (h) or 15 (min)

#### **Exemplars**

910 1010 1110 1135 1235 will only score B1 because it's not a fully correct method but 910 1010 1110+15 1135 1235 will score B2 because a full method is seen or implied

| 2(a) | 27 | B1 |  |
|------|----|----|--|
| 2(b) | 10 | B1 |  |
| 2(c) | 16 | B1 |  |
| 2(d) | 13 | B1 |  |

| Q   | Answer  | Mark  |                                |        | С       | omme   | ents   |      |   |
|-----|---|-------|--------------------------------|--------|---------|--------|--------|------|---|
| 3   | 3 × 65 or 195(p) or (£)1.95<br>or<br>3 × 110 or 330(p) or (£)3.30                     | M1    | 65 + 1                         | 10     | or 17   | 5(p) ( | or (£) | 1.75 |   |
|     | Adds all six items their (3 $\times$ 65) + their (3 $\times$ 110)                     | M1dep | 3 × the                        | eir (6 | 5 + 110 | 0)     |        |      |   |
|     | No <b>and</b> (£)5.25 or 525p   | A1    | oe<br>eg She will be 25p short |        |         |        |        |      |   |
|     |   |       |                                |        |         |        |        |      |   |
|     | (£)5 – at least two items eg $(£)5$ – 220   | M1    | Cost of                        |        | S       |        |        |      |   |
|     |   |       | iten                           | าร     | 0       | 1      | 2      | 3    |   |
|     |   |       |                                | 0      |         |        | 220    | 330  |   |
| 3   | Adds up the rest of the six items   | M1dep |                                | 1      |         | 175    | 285    | 395  |   |
| Alt |   |       | D                              | 2      | 130     | 240    | 350    | 460  |   |
|     |   |       |                                | 3      | 195     | 305    | 415    | 525  |   |
|     | No <b>and</b> correct amount of money left <b>and</b> correct cost of remaining items | A1    | oe<br>eg No a<br>or No a       |        |         |        |        |      | - |

Condone poor or mixed money notation for the first two marks eg 195 + 3.3 In the alt method there are many possible combinations to get the A1, but their answers will always be within 25p of each other so check this first

|       |   |      | ·                                      |
|-------|---|------|--|
| 4(a)  | q | R1   | Ignore working which may be for 4(b)   |
| -τ(α) | 3 | , D, | I ignore working which may be for +(b) |

| Q    | Answer     | Mark | Comments  |
|------|------------|------|---|
| 4(b) |            |      | Numbers arranged in ascending or descending order <b>and</b> a clear indication that 9 is the middle number |
|      | 5 7(9)9 10 | B1   | A clear and complete statement that 9 is the middle number when you arrange them in order                   |

Any incorrect working eg wrong order/ wrong numbers/ selecting both 9s or (9 + 9)/2 is B0 A clear indication of 9 being the middle could be eg by eliminating the numbers either side in the ordered list If there is an explanation rather than a demonstration, then both parts of the explanation are needed in 9 is the middle number is not enough

| 5    | T, T, F, T   | В3 | B2 3 correct<br>B1 2 correct  |
|------|--|----|---|
|      |  |    |   |
| 6(a) | F  | B1 |   |
|      | Square   | B1 |   |
|      |  |    |   |
| 6(b) | 9  | B1 |   |
|      | cm <sup>2</sup>  | B1 |   |
|      |  |    |   |
| 7(a) | Bar of height 4 labelled Coffee or C and Bar of height 5 labelled Juice or J (in either order but with a gap of 1 square between all bars) | B2 | B1 One of the bars labelled and correct or B1 Diagram fully correct but missing or incorrect label(s) or B1 Diagram fully correct but no gaps or incorrect gaps |

# Additional guidance

If in doubt please escalate the clip

| 7(b) | 7 (boys)    | B1   |  |
|------|-------------|------|--|
|      | their 7 – 4 | M1   | Subtraction may be implied by correct ft answer of their 7 – 4 |
|      | 3           | A1ft | ft B0M1 but must be integer answer for A1                      |

#### Additional guidance

The 7 may be seen on the answer line for B1 and condone even if says 7 more boys If they misread the table for girls ie use 5, 7 or 9 girls then can award up to max of B1M1A0 4-7 is acceptable for B1M1 and if it is followed by 3 will gain all the marks Answer only is full marks

| Q    | Answer  | Mark | Comments   |
|------|---|------|--|
| 8(a) | 15  | B1   |  |
| 8(b) | $30 \div 6 (= 5)$ or $30 \div 3$<br>or $(15 - )\frac{15}{3}$<br>or $15 \div 3 (\times 2)$ | M1   | oe eg $360 \div 30$ (= 12) and $(180 - 60) \div$ their 12 eg $180 - 60$ (= 120) and $\frac{\text{their } 120}{360} \times 30$ may be using their (a) for 15 (but not an angle) |
|      | 10  | A1ft | ft their (a) – 5 or their (a) $\div$ 3 $\times$ 2 but must be integer answer for A1  |

An answer of 5 would score M1

In the live marking you can scroll up to the pie chart and their answer to part (a) so that you can follow through

Please check the diagram and part (a) for any relevant working

| Q  | Answer  | Mark | Comments  |  |  |
|----|---|------|---|--|--|
|    | Decimals  |      |   |  |  |
|    | $(\frac{1}{10} =) 0.1 \text{ or } (11\% =) 0.11$  | M1   |   |  |  |
| *9 | $(\frac{1}{10} =) 0.1$ and $(11\% =) 0.11$  | A1   | oe  |  |  |
|    | Converting 1/10 and 11% to decimals with at least one right and arranging in correct ft order for <b>their</b> decimals | Q1   | Strand (ii) $SC1 \frac{1}{10}, 11\%, 0.2 \text{ with no working}$ |  |  |

|             | Percentages  |    |   |
|-------------|--|----|---|
|             | $\left(\frac{1}{10}\right) = 10(\%) \text{ or } (0.2 =) 20(\%)$  | M1 |   |
| *9<br>Alt 1 | $(\frac{1}{10}$ =) 10(%) <b>and</b> (0.2 =) 20(%)  | A1 | oe  |
| All I       | Converting 1/10 and 0.2 to percentages (both with percentage signs) with at least one right and arranging in correct ft order for <b>their</b> percentages | Q1 | Strand (ii) $SC1 \frac{1}{10}, 11\%, 0.2 \text{ with no working}$ |

|             | Fractions  |    |   |
|-------------|--|----|---|
|             | $(0.2 =) \frac{2}{10}$ or $(11\% =) \frac{11}{100}$  | M1 | oe fraction   |
| *9<br>Alt 2 | $\frac{10}{100}$ and $\frac{20}{100}$ and $\frac{11}{100}$   | A1 | oe three correct fractions with common denominator                |
|             | Converting all numbers to fractions with a common denominator with at least one numerator right and arranging in correct ft order for <b>their</b> fractions | Q1 | Strand (ii) $SC1 \frac{1}{10}, 11\%, 0.2 \text{ with no working}$ |

The first mark is for any one correct conversion to another form

For Q1 the answer may be with the numbers in the original or converted format (or a combination)

The fractions in Alt 2 may contain decimals eg condone  $\frac{1}{10}$ ,  $\frac{2}{10}$ ,  $\frac{1.1}{10}$  for M1A1 (and, if ordered, for Q1)

No working – can score SC1 Q is dependent on at least M1

| 10(a) | 54.32 | B1 |  |
|-------|-------|----|--|
|-------|-------|----|--|

| Q     | Answer  | Mark  | Comments  |  |  |
|-------|---|-------|---|--|--|
|       | Listing the positions of hurdles  |       |   |  |  |
|       | Listing at least 3 'hurdles' eg 45, 80, 115, or 35, 70, 105, or 85, 120, 155, or 355, 320, 285,   | M1    | oe<br>Condone 1 error   |  |  |
| 10(b) | Complete list eg 45, 80, 115, 150, 185, 220, 255, 290, 325, 360, (400) or 85, 120, 155, 190, 225, 260, 295, 330, 365, (400) or 400, 355, 320, 285, 250, 215, 180, 145, 110, 75, 40, (0) | M1dep | oe Ascending or descending with max 1 error (may be more if cumulative) |  |  |
|       | 10  | A1    | SC1 10 with M0M0  |  |  |

|       | Adding consecutive distances  |       |                  |
|-------|---|-------|------------------|
| 10(b) | Adds at least 3 consecutive distances  45 + 35 + 35 +  or  35 + 35 + 35 +  or  + 35 + 35 + 40 | M1    | oe eg 45 + 70 +  |
| Alt 1 | Complete method shown with 9 lots of 35 ie  45 + 35 + 35 + 35 + 35 + 35 + 35 + 35 +           | M1dep | oe               |
|       | 10  | A1    | SC1 10 with M0M0 |
|       | 400 - (45 + 40) (- 315)   | M1    |                  |

|                | 400 – (45 + 40) (= 315)                    | M1    |  |
|----------------|--|-------|--|
| 10(b)<br>Alt 2 | their $315 \div 35$ or $35 \times 9 = 315$ | M1dep | 315, 280, 245, 210, 175, 140, 105, 70, 35, (0) in either order and allow 1 error (may be more if cumulative) |
|                | 10   | A1    | SC1 10 with M0M0   |

Question says you must show your working so answer only of 10 scores SC1 An answer of 10 requires a completely correct full method with no errors or omissions for 3 marks There are lots of equivalents to all three schemes so you will need to use your judgment Some answers are a combination of two schemes eg 45 + 35 + 35 = 115, 115 + 35 + 35 = 185 etc but if you only see one error in a full method then award M2

| Q  | Answer                                    | Mark     | Comments |
|----|---|----------|----------|
| 11 | 2 × 11 <b>and</b> 3 × 5<br>or<br>22 or 15 | M1<br>A1 | oe       |

2 x 11 = 22a and 3 x 5 = 15b is M1 because correct method seen first 22a + 15b is M0 because no correct method seen 37 followed by further work with algebra eg 37ab is M1A0, but just 37ab is M0A0 2(11) (+) 3(5) is M0 unless further correct work seen

| *12        | $\frac{10}{100} \times 200$ oe or 20 seen                       | M1    | $\frac{90}{100} \times 200 \text{ oe}$ or 180 is M2 |
|------------|---|-------|---|
|            | 200 – their 20 or 180 seen                                      | M1dep | 100   |
| 12         | 6   | A1    |   |
|            | Method shown for 90% of 200 and dividing their result by 30     | Q1    | Strand (iii)  |
|            | 1   |       |   |
| *12<br>Alt | $\frac{200}{30}$ or $\frac{20}{3}$                              | M1    | oe  |
|            | $\frac{10}{100}$ × their $\frac{200}{30}$ or $\frac{2}{3}$      | M1dep | oe  |
|            | 6   | A1    |   |
|            | Method shown for dividing by 30 and finding 90% of their result | Q1    | Strand (iii)  |

#### Additional guidance

Correct method with arithmetic error(s) is likely to score M2A0Q1

The **Q mark** needs a method that leads to 90% shown (not just 180 seen) **and** the division shown Answer of 6 only is M2A1Q0 180 seen, then answer of 6 scores M2A1Q0 20, 180 and 6 is Q0 but 20, 180 and ÷ 30 all seen scores Q1

and (200 - 20) / 30 scores Q1

If build-up or build-down is used for 90%, it needs to be complete and either correct or **full** method shown **Exemplars** 

10% = 20, 90% = 140 is M1M0 because 140 is incorrect and the full method is not shown

10% = 20,  $90\% = 9 \times 20 = 140$  is M1M1 as method shown

10% = 2, 90% = 18 is M0M0 because 2 is incorrect and the full method is not shown

10% = 200 / 10 = 2, 90% = 18 is M1M1 as method is shown and 18 is ft correct

| Q  | Answer | Mark | Comments  |
|----|--------|------|---|
| 13 | 3      | B2   | B1 8 seen as value of X for Set A or 3 seen as value of X for set A but different value for set B |

Condone 3 from ambiguous working eg 7 - 4 = 3, 5 - 2 = 3

The 8 or the 3 for B1 may be embedded eg 7 - 4 = 3 or 4 + 4 = 8

| 14    | 27 | B1   |  |
|-------|----|------|--|
|       | 81 | B1ft | ft their 27 $\times$ 3 Answers must be evaluated |
|       |    |      |  |
| 15(a) | 75 | B1   |  |

|       | (27 – 5) ÷ 2 | M1   | Condone omission of brackets   |
|-------|--------------|------|--|
| 45(1) | 11           | A1   |  |
| 15(b) | 3            | B1ft | ft (their 11 – 5) ÷ 2 if A0 awarded<br>SC1 –0.75<br>SC1 24.5 <b>and</b> 22 |

# Additional guidance

 $(27 \div 2 - 5 = 8.5, 8.5 \div 2 - 5 =) -0.75$  scores SC1

 $27 - (5 \div 2) = 24.5$ ,  $24.5 - (5 \div 2) = 22$  scores SC1, but 22 alone does not score SC1

If 11 is wrong then check for follow through eg  $27 \rightarrow 12 \rightarrow 3.5$  scores M0A0B1ft

 $(27 - 5) \div 2 = 12$  and 3.5 scores M1A0B1ft

Ignore further working and award full marks if an attempt at further terms is made after term of 3 seen If 3 is embedded, award M1A1B0

3, 11, 27 on answer line by any scheme is 3 marks

|                | 2x + 5 = 27  | M1 |  |
|----------------|--|----|--|
| 15(b)<br>Alt 1 | 11 or $2(2x + 5) + 5 = 27$ oe<br>or $(27 - 15) \div 4$ | A1 |  |
|                | 3  | A1 |  |

| 15(b)<br>Alt 2 | Two fully correct trials<br>eg any two of<br>$u_1 = 1$ , $u_2 = 7$ , $u_3 = 19$<br>$u_1 = 2$ , $u_2 = 9$ , $u_3 = 23$<br>$u_1 = 4$ , $u_2 = 13$ , $u_3 = 31$<br>$u_1 = 5$ , $u_2 = 15$ , $u_3 = 35$ | M1    |  |
|----------------|---|-------|--|
|                | Fully correct trial with first term 3 ie $u_1 = 3$ , $u_2 = 11$ , $u_3 = 27$  | M1Dep |  |
|                | 3   | A1    |  |

| Q  | Answer   | Mark | Comments   |
|----|--|------|--|
|    | Isosceles triangle with base on 9 cm line and vertex within 2 mm (ie in the circle on the overlay) | B2   | B1 for any isosceles triangle on the base with vertex within 2 mm of centre line or B1 for any side 7.5 cm long ± 2 mm or any arc 7.5 cm drawn ± 2 mm or 7.5 (cm) seen   |
|    | No <b>and</b> 1.2 (m) or 120 (cm) or No <b>and</b> 6 (cm) <b>and</b> 6.4 (cm)                      | B1ft | ft the vertical height of their triangle  Jack's height accurately drawn ± 2 mm on diagram and a decision stated or  Vertical height of their triangle may be stated and compared to Jack's scale height ie [6.2, 6.6] |
| 16 | 5-<br>4-<br>3-<br>2-<br>1-   |      |  |

Note that you can swap the overlay for a ruler or a length measurer but you need to do so each clip The overlay is only 6 cm high so if their triangle is taller you need to judge whether it is within 2 mm of the centre line

Condone lack of arcs for all three marks

Drawing Jack's height as  $6.4 (\pm 2 \text{ mm})$  may be used for comparison (use the length measurer to check it) An answer of No and [1.16, 1.24] with a diagram is likely to be all 3 marks

NB Must have a diagram to score the final mark

| Q            | Answer  | Mark | Comments  |
|--------------|---|------|---|
|              | Line from (08 00, 0) to (09 30, 60)   | B1   | Line need not be straight ± 1 small square                                    |
| 17(a)        | 1 cm horizontal line from their (0930, 60) or horizontal line ending at 1000  | B1ft | ± 1 small square  |
| (ω)          | Line from (10 00, 60) to meet the time axis between (11 06, 0) and (11 18, 0) inclusive or line from their (10 00, 60) down 6 cm and across 2.4 cm oe | B1ft | Line need not be straight ± 1 small square                                    |
| 17(b)        | Correct ft decision and reference to their graph or correct ft decision and correct ft time (±6 minutes) read from their graph                        | B1ft | Must be from a line that meets the time axis at least 6 mins after their 1000 |
| 17(b)<br>Alt | Correct ft decision and calculation of home time eg 60 miles at 50 mph = 1.2 hours 11 30 is 1.5 hours after 10 or 10 + 1.2 hours = 1112               | B1ft | ft from their 1000  |

#### Additional guidance – exemplars

These are B1:

Yes as he gets home at 1110 (1110 within one small square of his graph)

Yes he will see the show, I've shown it by my graph (line ends before 1130)

Yes my graph shows that Dan gets home by 1130 (line ends at (1112, 0))

No, see my graph (line ends after 1130)

Yes as after an hour, he has 10 miles to do at 50 mph which will take less than half an hour

Yes as he gets home at 1024 B1 ft mark (line ends at (1024, 0))

No as he gets home at 1145 (line ends at 1148 so within 6 minutes)

Yes my graph shows he gets home at 1130 (line ends at 1130)

No my graph shows he gets home at 1130 so he'll miss the first few minutes (line ends at 1130)

#### These are B0:

Correct graph in (a) then Yes he does get home by 11 30 (no reference to graph made)

Yes 50mph = 50 miles every hour. After 1 hour, 10 miles from home which equals 11 00 (incomplete)

He gets home at 1112 (no decision made)

Yes he gets home at 11.2 (incomplete eg needs to compare 11.2 with 11.5 or convert 11.2 correctly)

| Answer |             |           |         | Mark    | Comments  |
|--------|-------------|-----------|---------|---------|---|
| 4 15   | <b>12</b> 5 | <b>10</b> |         | В3      | B2 12 and/or 10 in correct position <b>and</b> any product that makes 60 in first column (not using 5 or 6)  B1 12 and/or 10 in correct position <b>or</b> any product that makes 60 in first column (not |
|        | 4<br>15     | 4 12      | 4 12 10 | 4 12 10 | 4 12 10 B3  |

Condone missing or incorrect 26s and 60s

# **Exemplars**

| 20 | 10 | 12 |
|----|----|----|
| 3  | 5  | 6  |

scores B1

| $2\frac{1}{2}$ | 12 | 10 |
|----------------|----|----|
| 24             | 5  | 6  |

scores B2

# Additional guidance

Assume lines are intended to be straight

|    | 4 <i>n</i> | M1 | Accept 4 $\times$ $n$ or $n \times$ 4 but not $n$ 4                  |
|----|------------|----|--|
| 20 | 4n + 2     | A1 | oe<br>eg $4 \times n + 2$<br>3n + n + 2<br>2(2n + 1)<br>SC1 $n4 + 2$ |

| *21a | Open circle at -2 with line going right to at least 4 or arrow (of any length) to the right | Q1 | Strand (i) If line is marked with any sort of circle at the RHS this is Q0 |
|------|---|----|--|
|------|---|----|--|

| Q   | Answer   | Mark | Comments  |
|-----|--|------|---|
| 21b | $3x \le 11 - 5 \text{ or } 3x \le 6 \text{ or } x - 2 \le 0$ | M1   | Working with = sign must be recovered to ≤ to gain any credit |
|     | $x \leq 2$   | A1   | Must have $x \le$ on answer line SC1 $x < 2$                  |

Just ≤ 2 scores M1A0

 $x \le 2$  seen in working, then incorrect answer is M1A0

Any inequality that is one step away from the correct answer is M1 eg  $x + 1 \le 3$ 

Embedded answer  $3 \times 2 + 5 \le 11$  is M0 unless further creditworthy work

Any slight error in notation eg  $x \le 2$  or  $x \le 2$  is M1A0

|    | $\pi \times 10^2 \times 4$  | M1 |  |
|----|---|----|--|
| 22 | $\pi \times 100 \times 4$ or $3.1 \times 100 \times 4$ or $31 \times 40$ or $124 \times 10$ | A1 | Any of these products or better Condone use of 3.14 or 3.142 or $\frac{22}{7}$ |
|    | 1240  | A1 | Accept 1256 or 1256.8 or 1257.() or 1260                                       |

#### Additional guidance

Further working eg  $\div$  10 or  $\div$  2 means an incorrect method has been used so M0 To get the first A1 the student must show that  $10^2 = 100$  which may be done as two products using 10